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QUICKLITE 1:

A DAYLIGHTING PROGRAM

FOR THE TI-59 CALCULATOR

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ABSTRACT

This paper presents a set of daylighting programs that can be run on a TI-59 hand calculator. The paper gives the program listings, the step-by-step procedures for using the programs, worksheets, and a worked sample problem.

The programs calculate interior horizontal illumination levels or daylight factors from a window. The user can specify the location of the calculation point, or, if a printer is available, the locations of a grid of points. Calculations can be performed for both CIE clear and overcast sky conditions.

The direct sky component calculation uses Rivero's approximation for window transmission. The interreflected component calculation uses a split-flux approximation.

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INTRODUCTION

Daylighting is now considered one of the most promising energy conservation strategies for nonresidential buildings. Although substantial savings in both electrical energy and peak power demand are possible, potential savings may not be achieved given the present state of daylighting design procedures. A major obstacle to the effective utilization of daylighting is the lack of accurate and simple procedures for daylighting design and analysis.

Three types of design tools have been used to predict interior daylight illumination: scale models, graphic techniques, and calculations. A detailed discussion of the strengths and limitations of each is beyond the scope of this paper; we focus here on computational approaches.

Calculations can provide a fast and accurate assessment of illumination levels for typical room and glazing design. Present procedures for calculating daylight illumination can be divided into two categories: simplified procedures, which often make simplifications and assumptions that may reduce flexibility and accuracy, and large-scale computer programs, which, although they may be more flexible and accurate, require the preparation of detailed input data and access to computers or time-sharing computer facilities. There is a need for a calculation procedure that combines the speed, low cost, and ease of the simplified methods with the flexibility and accuracy of the large computer models.

This paper describes a calculation procedure, using a programmable hand calculator, that is a major step toward that goal.

QUICKLITE 1 PROGRAM DESCRIPTION

Quicklite 1 will predict daylight illumination at any point within a room. The methodology and algorithms used in the development of this program are documented in a previous paper. Further details and additional program capabilities will be described in a later publication.

The program utilizes the CIE sky luminance distribution functions

for the overcast and clear skies. ^{3,4} The light reaching the interior point being considered is separated into two components. Light arriving directly from the sky (Sky Component or SC) is calculated using a source area formula. Light reflected from external and internal surfaces (Reflected Component or RC) is calculated using the split flux approach. The total for these two components is given as either the daylight factor (the ratio of illumination at the reference point to illumination on a horizontal surface from the unobstructed sky) or illumination (in footcandles) for the point(s) being considered. This paper describes the use of the program to calculate daylight illumination for a simple window without obstructions or sun-control devices. The program can also be used to solve more complex daylighting problems; however, the length of this paper limits their inclusion. Solutions to these problems are described in reference 2.

Quicklite 1 has been designed to be accurate, simple, and relatively fast-running. The output compares well with other daylighting calculation procedures as well as with a series of physical scale-model measurements. However, it must be remembered that no calculation procedure, no matter how accurate, can duplicate all the complexities that daylighting poses. In most cases we seek comparative performance levels rather than absolute quantitative results. We must also remember that the non-quantifiable aspects of lighting design are equally important and that nothing can substitute for good design judgment.

- I: SKY COMPONENT PROGRAM: This program uses the TI-59's master library. If multiple point calculations are desired for a single program execution, the PC-100 printer must be used.
- Step 1: Repartition the calculator memory by entering 5 and then pressing 2nd OP 17.
- Step 2: Determine if sky condition is clear or overcast, then read appropriate program into calculator. The clear sky program will require reading sides 1, 2, and 3, while the overcast sky program requires reading only sides 1 and 2.
- Step 3: a) Enter window transmission at normal incidence (90° to the plane of the window).

NOTE: Steps (3b-3e) should be executed only for the clear sky program.

b) Enter the normalization factor (N_{SC}) which is the ratio of illumination on a horizontal plane to the luminance at the zenith. This factor is a function of solar altitude and is given as follows:

Solar Altitude	N _{sc}
10°	3.654
20,000,000	3.565
30 %	3.235
40°, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	2.741
50°	2.178
60°	1.632
70%	1.159
80, %	0.782
90°	0.503

- c) Enter window azimuth angle (in degrees), which is the angle that a line normal to a vertical window makes with south (which is taken to be 0°). Clockwise rotation from south is measured as positive while counter-clockwise rotation is measured as negative. (See Figure 1)
- d) Enter solar azimuth angle (in degrees), which is the azimuthal angle of the sun from south. Here again clockwise rotation from south is measured as positive while counter-clockwise rotation is measured as negative. (See Figure 1)

NOTE: This program does not compute the effect of direct sun in the room. There will be direct sun at some point in the room for an obstructed window if the absolute value of the difference between the window azimuth and solar azimuth is less than 90°.

e) Enter solar altitude (in degrees from horizontal). (See Figure 1.)

- Step 4: Enter the location and size of the window and the workplane height at which illumination is to be calculated. A rectangular coordinate system is used to locate the window as well as the calculation point(s) (see Figure 2). The origin of this coordinate system should be placed at the lower left-hand corner of the window-wall's interior face. When facing the window from the interior of the room, the X-axis will run along the floor perpendicular to the window-wall. The Y-axis will run to the right, along the intersection of the floor and the window-wall. The Z-axis will point straight up. location and size of the window is described by four values: Y_{left} and Y_{right} represent the respective distances of the left- and right-hand sides of the window from the Z-axis, $\mathbf{z}_{\mathtt{bottom}}$ and $\mathbf{z}_{\mathtt{top}}$ represent the respective distances of the bottom and top of the window from the floor. Finally, the height of the calculation point(s) above the floor (Z_D) must be determined. For most office tasks Z_p is assumed to be 2.5 feet. Figure 2 illustrates these relationships.
- Step 5: Determine if the output is to be calculated in units of daylight factor or illumination. To calculate the daylight
 factor, the number 1 must be stored in register 35. To
 calculate illumination, the appropriate horizontal illumination
 from the sky (E_{sky}) must be stored in register 35. This value
 can be found in Figure 36A, B, C, or D in the IES Recommended
 Practice of Daylighting, in reference 2, or can be taken from
 any other source of measured or calculated illumination data.

NOTE: To calculate values for a single point, proceed to steps 6a and 7a. If a printer is available, multiple points on a rectangular grid may be calculated and printed by proceeding to steps 6b and 7b.

Single Point Procedure:

Step 6a: Enter the location of the point at which the daylight factor or illumination calculation is to be made. Y is the distance from the measurement point to the wall to the left of the window. X is the distance from the measurement point to the window-wall. (See Figure 2)

Step 7a: Calculate the sky component by pressing 2nd B'.

Multiple Point Procedure:

Step 6b: Enter the corner locations of the rectangular grid of calculation points. Y and Y are, respectively, the distances from the wall at the left of the window to the closest and the farthest columns of calculation points. X_{\min} and X_{\max} are, respectively, the distances from the window-wall to the closest and the farthest rows of calculation points. (See Figure 2) Finally, the number of calculation points for the Y-column (N_y) , and X-row (N_x) , must be determined. N_y and N_z include the corner points and thus must be greater than or equal to two. Setting N_y or N_z to one will result in a "divide by zero" error.

Step 7b: Calculate the sky component values by pressing 2nd D'. Run time for this option is approximately 1.2 minutes per point for overcast sky and 3 minutes per point for the clear sky.

General Notes: Sky Component Program

- 1) It is unnecessary to re-enter all the input data for repeated calculations. Only those input values entered in step 6a or 6b must be re-entered to rerun the program. All other input values need to be changed only if their new values differ from those used in the previous run.
- 2) All inputs that relate to distance (such as width of the window) may be entered in any unit, English or metric, so long as the user is consistent.

- 3) If a printer is being used, it is highly advisable to make a list of the register contents before running the program. To obtain a permanent list of the data registers, enter 30 and then press INV LST before executing step 7a or 7b. (For register assignments see Figure 6.)
- 4) Figure 4 summarizes the steps required to enter and run the Sky Component program.

REFLECTED COMPONENT PROGRAM: This program uses the TI-59's master library. The PC-100 printer is optional.

- Step 1: Repartition the calculator memory by entering 3 and then pressing 2nd OP 17.
- Step 2: The reflected component requires reading sides 1 and 2.
- Step 3: Enter window width and height.
- Step 4: Enter room width, depth, and height plus the height of the window sill above the floor.
- Step 5: Enter normal incidence window transmission.
- Step 6: Enter reflectance of ceiling, floor, glass and walls as well as exterior ground.
- NOTE: There are four options for output from this program. The appropriate option must be chosen from steps 7a, b, c, or d.
- Step 7a: To calculate the daylight factor from the reflected component under an overcast sky, enter the window factor (f_s). The window factor is the ratio of the light flux entering the window from the sky to the light flux on an exterior horizontal plane. For an unobstructed sky $f_s = .39$.
- Step 7b: To calculate the illumination level from the reflected component under an overcast sky, enter the window factor (f_s) as in step 7a and the horizontal illumination from the sky (E_{sky}), which can be found from Figure 36A in reference 5.
- Step 7c: To calculate the daylight factor from the reflected component under a clear sky, enter the window factor (f_s) , the horizontal illumination from the sky (E_{sky}) from Figure 36B, C, or D in reference 5, and the horizontal illumination from the sun

 (E_{sun}) from Figure 37A in reference 5. The window factor for a clear sky is a function of solar altitude as well as of window azimuth from the sun and is given below.

Solar		Window	Azimuth	from	Sun
Altitude	0°	45°	90°	135°	<u>180</u> °
10°	.68	. 65	.50	.35	.32
20°	.72	.67	.50	. 33	.28
30°	.73	.70	.50	.30	.27
40°	.74	.69	.50	.31	.26
50°	.73	.68	.50	.32	. 27
60°	.70	.66	.50	. 34	.30
70°	.66	.62	.50	.38	.34
80°	.59	.56	.50	.44	.41
90°	.50	.50	.50	.50	.50

Step 7d: To calculate the illumination level from the reflected component under a clear sky, proceed as in step 7c, but a different label is pressed for the resulting answer.

General Notes: Reflected Component

- 1) A single average value for the reflected component is computed for the entire room.
- 2) It is unnecessary to re-enter all the input data for repeated calculations. Change only those values entered in steps 3 through 6 that differ from the previous run. Then execute the program beginning at step 7.
- 3) If a printer is being used, it is highly advisable to make a list of the register contents before running the program. To obtain a permanent record of the data registers, enter 15 and then press INV LST before executing step 7. (For register assignments see Figure 7.)
- 4) Figure 5 summarizes the steps required to enter and run the Reflected Component program.

SAMPLE PROBLEM

Calculate the illumination for the room shown in Figure 3, which is

30 feet wide, 20 feet deep, and 8.67 feet high and which has one large window, 5 feet high by 28 feet wide. The window is 2 feet above the floor and centered on a wall facing due west. Glazing consists of two layers of 1/4 inch clear glass having a combined normal daylight transmission of 78%. The ceiling has a reflectance of 80%, the floor 20%, the wall 50%, and the glass 14%.

Illumination is to be calculated under both clear and overcast conditions. The sun is assumed to be due south at an altitude of 40° . The horizontal illumination from the sky ($E_{\rm sky}$) is 1400 footcandles under overcast sky conditions (from Figure 36A in reference 5) and 1200 footcandles under clear sky conditions (from Figure 36C in reference 5). The horizontal illumination from the sun ($E_{\rm sun}$) is 4800 footcandles (from Figure 37A in reference 5). Finally, a three-by-three calculation grid (9 calculation points) was selected, each edge of the grid being five feet from the nearest wall. (See Figure 3)

The sky component program for both clear and overcast skies was run first. Figure 6 shows the sample input and output from this example in which both the data register contents and results are identified. The reflected component program for both sky conditions were then run. Figure 7 shows the sample input and output from this run; here again data register contents and results have been identified. Finally, the sky component and reflected component values were added to determine overall illumination values. Results from the overcast sky example are shown in Figure 8. Notice that the illumination is symmetric about the center line of the room as expected. Results for the clear sky example are given in Figure 9. Here the change in sky luminance with azimuth results in an asymmetrical illumination distribution across the room. In each case the reflected component is calculated as an average value throughout the room. This approximation will generally result in an overestimate of daylight illumination in the back of the room. Comparison between reflected component results from the average value approach described here, and a more detailed calculation is given in reference 2.

CONCLUSION

A relatively accurate, simple, and fast procedure for calculating interior daylight illumination has been presented. It is hoped that the application of this procedure will encourage the use of daylighting, placing it in a proper relationship to other design considerations. A lengthier version of this paper that includes a detailed program description, user instructions, and several worked examples (which include external obstructions, overhangs, direct sun in room, etc.) will be available from the authors at the address below. This calculation procedure is one of several daylighting design tools now under development as part of the LBL/DOE Daylighting Program. For information on the availability of other daylighting design tools, write to:
Windows and Daylighting Program, Lawrence Berkeley Laboratory,
Building 90, Room 3111, Berkeley, California 94720.

ACKNOWLEDGEMENTS

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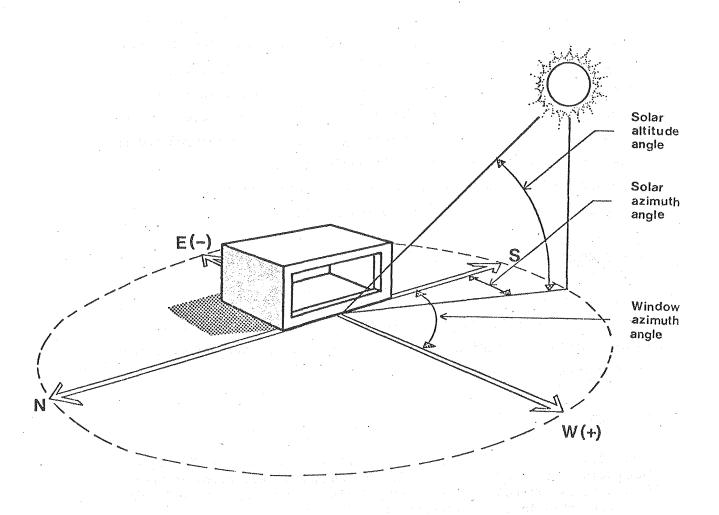


FIGURE 1. SITE COORDINATE SYSTEM FOR PROGRAM

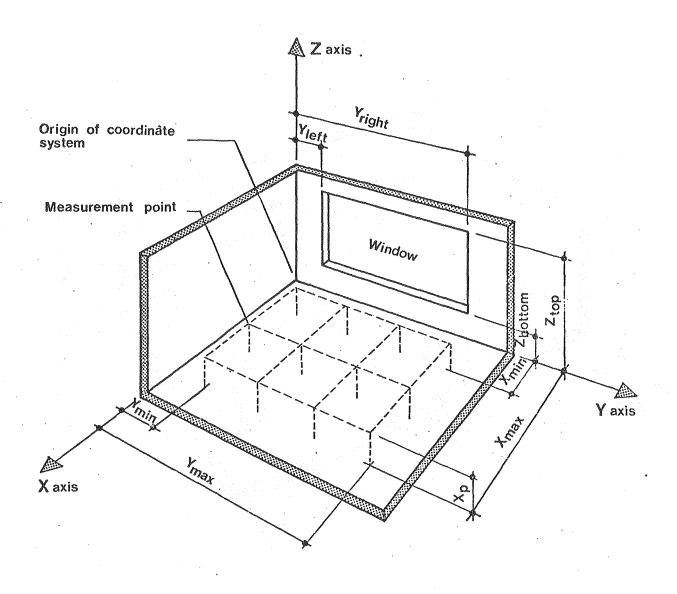


FIGURE 2. ROOM COORDINATE SYSTEM FOR PROGRAM

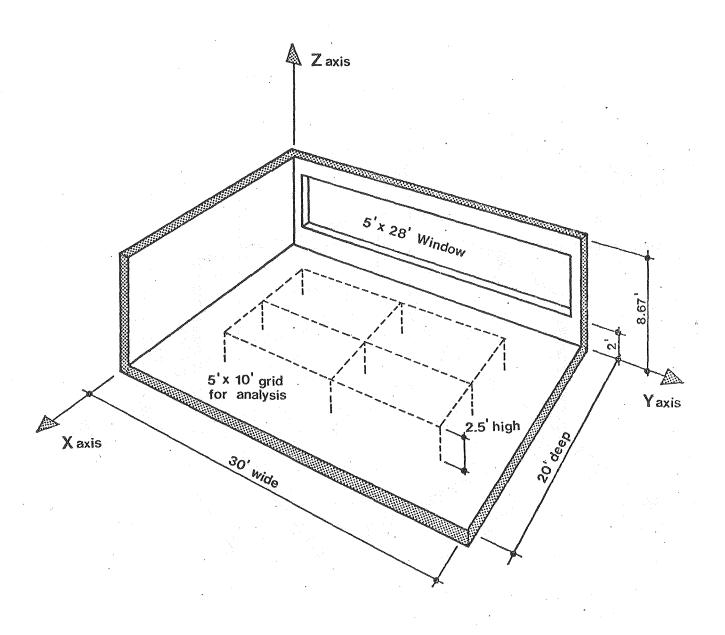


FIGURE 3. EXAMPLE ROOM

	PROCEDURE	ENTER	PRESS	DISPLAY
1	Repartition calculator	5	2nd OP 17	559.49
2	Clear Sky: Read sides 1, 2 & 3	1,2,3	2nd INV WRITE	1,2,3
	Overcast Sky: Read sides 1 & 2	1,2	2nd INV WRITE	1,2
3a	Enter Window Transmission		A	1.018T _o
Note:	Steps 3b-3e should be executed for	To	^	1.01010
Note.	clear sky only			
21			2/0	.,
3b	Enter Normalization Factor	N _{sc}	R/S	N _{sc}
3с	Enter Window Azimuth (in degrees)	AZ _{window}	R/S	AZ _{window}
3d	Enter Solar Azimuth (in degrees)	AZ _{solar}	R/S	^{AZ} solar
3e	Enter Solar Altitude (in degrees)	ALTsolar	R/S	ALT _{solar}
4	Enter Y _{left}	Y _{left}	STO 3Ø	Y _{left}
	Enter Y _{right}	Yright	STO 31	Y _{right}
	Enter Z _{bottom}	Z _{bottom}	STO 32	Z _{bottom}
	Enter Z _{top}	Z _{top}	STO 33	Z
	Enter Z _p	z _p	STO 34	Z _p
5	To calculate Daylight Factor: Enter 1	1 or E _{sky}	STO 35	l or E _{sky}
	To calculate Illumination: Enter E _{sky}			
Note:	For Single Point Calculation:			
6а	Enter Y _p	Yp	STO 36	Yp
	Enter X _p	Х _р	STO 37	Х _р
7a	Run Program	enna	2nd B'	s.c.
Note:	For Multiple Point Calculations:			
6b	Enter Y _{min}	Y _{min}	STO 38	Y _{min}
10000000000000000000000000000000000000	Enter Y _{max}	Ymax	STO 39	Ymax
	Enter X _{min}	X _{min}	STO 4Ø	X _{min}
	Enter X _{max}	X _{max}	STO 41	Xmax
	Enter number of points along Y axis	N _y	STO 42	N.
	Enter number of points along X axis	N _x	STO 43	N×
7b	Run Program	-	2nd D'	s.c.

FIGURE 4. SKY COMPONENT PROGRAM WORKSHEET

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
1	Repartition calculator	3	2nd OP 17	719.29
2	Read sides 1 & 2	1,2	2nd INV WRITE	1,2
3	Enter Window Width	Width _{win}	S TO 1 5	Widthwin
aning control of the	Enter Window Height	Height _{win}	STO 16	Height _{win}
4	Enter Room Width	Width _{rm}	STO 17	Width _{rm}
description of the second of t	Enter Room Depth	Depth _{rm}	STO 18	Depth _{rm}
	Enter Room Height	Height _{rm}	STO 19	Height rm
منخدستا	Enter Window Sill Height	Height _{sill}	STO 20	Height sill
5	Enter Window Transmission	T _o	STO 21	T _o
6	Enter Ceiling Reflectance	ceiling	STO 22	ceiling
	Enter Floor Reflectance	floor	STO 23	floor
The state of the s	Enter Glass Reflectance	glass	STO 24	glass
	Enter Wall Reflectance	wall	STO 25	wall
	Enter Ground Reflectance	ground	STO 26	ground
7a	Daylight Factor for an overcast sky:			
othichadasa (control of the control	Enter Window Factor	fs	STO 27	fs
	Run Program	_	Ą	R.C.
7ъ	Illumination for an overcast sky:			
	Enter Window Factor	fs	STO 27	fs
PRESENTATION OF THE PROPERTY O	Enter Illumination from sky	E _{sky}	STO 28	E _{sky}
	Run Program		В	R.C.
7c	Daylight Factor for a clear sky:		in the state of th	
	Enter Window Factor	f _s	STO 27	fs
	Enter Illumination from sky	E _{sky}	STO 28	E _{sky}
positratina	Enter Illumination from sun	Esun	STO 29	Esun
	Run Program	_	C	R.C.
7d	Illumination for a clear sky:		-	
	Enter Window Factor	fs	STO 27	fs
	Enter Illumination from sky	E _{sky}	STO 28	E _{sky}
National Control of Co	Enter Illumination from sun	Esun	STO 29	E _{sun}
	Run Program	_	D a	R.C.

FIGURE 5. REFLECTED COMPONENT PROGRAM WORKSHEET

nit more and a supplementary of the supplementary o	ÔVERCAST SKY		CLEAR SKY			
VARIABLE	INPUT	MEMORY #	INPUT	MEMORY #		
Yleft Yright Zright Zbottom Ztop Zp Esky Xp Xp Yman Ymax Xmin Xmax Xmin Xmax Xmin Xmax ALTolar	1. 29. 2. 7. 2.5 1400. 0. 0. 5. 25. 5. 15. 3. 0.79404 0. 0.	30 31 32 33 34 35 36 37 38 39 41 42 43 44 45 46 47 48	1. 29. 2. 7. 2.5 1200. 0. 0. 5. 25. 25. 3. 3. 3. 0. 79404 2. 741 90. 0. 40.	30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48		
	OUTPUT		OUTPUT	my sky Nase		
	5. 5. 88. 96117803	Y SC	5. 5. 77. 88657598	X ************************************		
	5.	X	5.	X		
	15.	Y	15.	Y		
	102. 7729127	SC	104. 8656102	SC		
	5.	x	5.	X		
	25.	Y	25.	Y		
	88. 96117803	sc	96. 82265492	SC		
	10. 5. 21. 5 263186	X SC	10. 5. 25. 84613883	X Y SC		
	10.	X	10.	X		
	15.	Y	15.	Y		
	27. 28921538	SC	37. 53479146	SC		
	10.	X	10.	X		
	25.	Y	25.	Y		
	21. 5263186	SC	32. 852973	SC		
	15.	X	15.	X		
	5.	Y	5.	Y		
	8. 23775761	SC	12. 04242839	SC		
	15.	X	15.	X		
	15.	Y	15.	Y		
	10. 48444276	SC	16. 81735902	SC		
	15.	X	15.	X		
	25.	Y	25.	Y		
	8. 23775761	SC	15. 02274864	SC		

FIGURE 6. INPUT AND OUTPUT FOR SKY COMPONENT PROGRAM

	OVERCAST SKY		CLEAR SKY			
VARIABLE	INPUT	MEMORY #		INPUT	MEMORY #	
WIDTHwin HEIGHTwin WIDTHrm DEPTHrm HEIGHTsill To Ceiling Pfloor Pglass Pwall Pground FS Esky Esun	28. 5. 30. 20. 8.67 2. 0.78 0.2 0.14 0.5 0.2 0.39 1400. 0.	15 16 17 18 19 20 21 22 23 24 25 26 27 28 29		28. 5. 30. 20. 8.67 2. 0.78 0.2 0.14 0.5 0.2 0.5 1200. 4800.	15 16 17 18 19 20 21 22 23 24 25 26 27 29	
	OUTPUT	No. 1		OUTPUT		
R.C.	27.	RC		61.	RC	

FIGURE 7. INPUT AND OUTPUT FOR REFLECTED COMPONENT PROGRAM

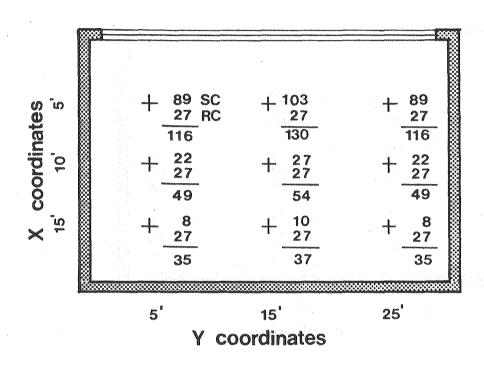


FIGURE 8. OVERCAST SKY ILLUMINATION VALUES (fc) FOR EXAMPLE ROOM

FIGURE 9. CLEAR SKY ILLUMINATION VALUES (fc) FOR EXAMPLE ROOM

050 65 × 105 42 STD 160 24 24 215 36 36 051 43 RCL 106 22 22 161 95 = 216 69 DP 052 11 11 107 00 0 162 44 SUM 217 06 06 053 55 ÷ 108 42 STD 163 19 19 218 03 3	0012345678900123456789000000000000000000000000000000000000	L H T T T S T T S T T T T S T T T T T S T	056789012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234	18 18 18 18 19 19 19 19 19 19 19 19 19 19		0-400456700-00045670000-00045670000-00045670000-000-000-000-000-00-00-00-00-00-00-	108 07 LX 04 L0 VM 4 L0 S0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2 0 2 1 0 1 2	5667890123456789001234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234567890012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789012345678901234567890123456789001234567890012345678900123456789000000000000000000000000000000000000	799 L2M0780 04 08000LP 2 TL100GTZ7XLTV 4 P 4L7 6 P 99 83240 98 8 2 S GSLN 1 + 2 TL100GTZ7XLTV 4 P 4L7 6 P 06 4 2 4 10 9 0 4 2 0 4 6 8 5 2 5 2 5 2 5 2 5 2 5 7 5 9 0 4 9 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 4 3 6 0 6 0 6 0 4 3 6 0 6 0 6 0 4 3 6 0 6 0 6 0 6 0 6 0 6 0 6 0 6 0 6 0 6
050 65 × 105 42 STD 160 24 24 215 36 36 051 43 RCL 106 22 22 161 95 = 216 69 DP 052 11 11 107 00 0 162 44 SUM 217 06 06	046 047 048	02 2 65 × 43 RCL	101 102 103	04 4 42 STO 09 09	*	156 158 158	43 RCL 11 11 65 ×	211 212 213	05 5 69 DF 04 04
أيت أيلاً أيسانيا في المرابع ا	050 051 052	65 × 43 RCL 11 11	105 106 107	42 STO 22 22 00 0		160 161 162	24 24 95 = 44 SUM	215 216 217	36 36 69 DP 06 06

0-1204567890-1204567890-1204567890-1204567890-1204567890 222222222222222222222222222222222222	15 P 4 L 9	567890123456789012345678901234567890123456789012345 77777888888899999999990000000011111111122222 2222222222	÷ (L6 RO-1)=T4LLR DML RVLMR VZO L9M6D L VZ6XL2D0L8D6L1M 533651452121464727274712270343946146XL2D0L8D6L1M 533621214647272747122703439462732290344400434344444	378 379 380	1X8L BD L2 L4 03 - VEX 1X8L BD L2 L4 03 - VEX 1X8L BD L2 1X8	567890-234567890-23667800-2360000000000000000000000000000000000	62305365537520213153655375202271326131536132614 6230536553752021315365537520227132614 62305365537520227132614 62374365537520234080132614 62374365537520227132614 614 614 614 614
267 268 269	43 RCL 41 41 75 -	323 324	36 36 43 RCL 41 41	377 378 379	43 RCL 34 34 54)	432 433 434	42 ST 06 (61 GT

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(.32 - L8
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REFLECTED COMPONENT PROGRAM (cont.)

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