



* T I P P C N O T E S *

v7n10, 1982.

NEWSLETTER OF THE TI PERSONAL
PROGRAMMABLE CALCULATOR CLUB.

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I should start here with the classical "I have some good news and some bad news. Now for the good news..." Well, let's reverse this order and get the bad news out of the way as soon as possible: Electronic News, September 27, 1982, page 57, carries an article with the title "TI Portable CPU Line May Dump Top Calculator." Then it goes on saying: "Texas Instruments has decided to withhold its top of the line TI-88 hand-held keystroke-programmable calculator, and will scrap it altogether as it shifts priorities to a family of hand-held computers it will unveil shortly. The article is far too long to be reproduced here in its entirety. But I learned from it that TI has opened up eight new facilities for the production of the TI-99/4A home computer or for making its components and that their total output is now 30,000 units per week. The real reasons for the demise of the 88 are probably a little more complex than TI explains in these simple terms of "shifting priorities", but the net result is that the 59 will be their top of the line machine. Requiescent in Pace TI-88.

The Digit Reversing puzzle generated so much interest that we dedicated several pages to it. In fact, the original number of pages I had for this issue totaled 31. By some judicious reducing and editing (hm,hm) we managed to get everything on 14 pages.

There are also several solutions to Myer Boland's Let Me Count the Ways puzzle. But the real star problem was the Pie Chart drawing contest. So far, and contrary to what I say on pages 6 & 7, I have received three solutions: The one published here and written by Robert Prins in the Netherlands, one by Lars Nilsson in Sweden and a third one by Michael Sperber in West Germany. Although slow all three, as expected, they neatly solve the problem and produce pie charts in Graphics Mode. My hat off to the three geniuses.

As I said in last issue, don't despair if you haven't seen your contribution appear in these pages yet. I am sending all as-yet-unpublished articles to Palmer Hanson for his consideration. But don't stop sending Palmer new ones. Let Palmer know that you support him, not by words, but by deeds. What he needs is programs, articles, neat tricks, in short publishable material.

Also, send in your dues early this year, so that Palmer will know what funds he can count on for 1983. You will find a subscription form with your address already on it. Correct it if necessary. I still have a few sets of back issues available on a first come first served basis. All those who received the Notes free, please send in your subscription form to Palmer Hanson with a note telling him of the arrangement and the reason why you want it to continue. Thank you.

Now, for the traditional (and expected of me) swan song: It has been lots of fun to get to know all of you, and especially the ones who repeatedly sent in good contributions which were subsequently published in these pages. My sincerest thanks and admiration for so much talent and dedication. I learned a lot from you.

I only hope now that we will not become strangers and that we will keep in contact.

Cordially,

Jmaunay

IN THIS ISSUE:

LET ME COUNT THE WAYS, Boland, Hanson, Buechner, Gustavsson, Snyder, Kempf	2
CALCULUS BY CALCULATOR, M. Weir	2
DIGIT REVERSING PUZZLE, Otto, Patzer, Hanson Adams, Coda, Williamson, Weinberger, Snyder, Mattheson, Bauer, Hamlin, Ristanovic, Klein, Sorensen, Kempf	3
PIE CHARTS, Robert Prins	6
CIRKELDIAGRAM, Lars Nilsson	7
TI-59 INTEGRATION, Henrik Klein	10
ARRIVAL OF THE STORM, Michael Sperber	14
DIGIT REVERSER II, Herman Stevens	14
WANTED, Girola	14

LET ME COUNT THE WAYS, by Myer Boland provoked a lot of reaction. I was unaware that there were so many puzzlers. The original programs Myer sent me were the following:

- 1) PAU + PI COS ABS = LBL A RAD CMs RST
- 2) PAU + CE DIV CE = LBL A CMs RST
- 3) PAU SUM+ RST LBL A CMs RST (this is the one I gave as a preview)
- 4) + OP E') PAU RST LBL A CMs CLR INV LNX PAU RST
- 5) INV LOG X (OP E' INV LOG) = LOG PAU RST LBL A CMs CLR INV LNX PAU RST
- 6) EE INV EE CP + X:T) + INV P/R = X=T RST PAU RST LBL A RAD FIX 0 RST

As you can see, some of them are long and among them you will find some of the fastest routines. As we just wanted other possible routines and didn't want this simple thing to degenerate into a speed contest, no rating is given neither for speed nor for briefness. Maybe elegance would be a good criterium. If that is accepted, my vote carries # 6, where Myer uses the device CP + X:T to get the number on both sides of X:T, so as to use to X=T to prevent repeating numbers. Nice!

Palmer Hanson says that Myer's sequence starts with zero, not with 1 as stated. What is more, if Myer's routine contains anything else than a zero, it will flash that number first and then flashes numbers incremented from it. Palmer sends three routines of his own:

- 1) SUM+ PAU RST LBL A CMs RST, which is the shortest of the three, but also the

CALCULUS BY CALCULATOR.- Maurice Weir, Prentice-Hall, Inglewood Cliffs NJ, 07632, 387 pages, softcover, \$ 15.95. Published Sept.22, 1982.

Maurice, as most of you are aware of by now, is a PPC member. He is also a mathematics professor at the Naval Postgraduate School in Monterey, California. He has written several books on the use of programmable calculators in mathematics education. This one again is superb.

The book contains six chapters:

1. Coordinates, Lines and Polynomial Functions.
2. Functions, Limits and Continuity.
3. Differentiation.
4. Integration.
5. Differential Equations.
6. Infinite Series.

Appendix A contains TI-59 programs

slowest: it counts only up to 44 in a minute.

- 2) OP 10 + PAU PLB A PI RST, which is longer but counts up to 88 in a minute.
- 3) LBL A CP X:T COS + PAU RST counts up to 75 in a minute.

Bill Buechner has two routines to offer. The first one duplicates exactly Palmer's # 1, but the second one goes like: = PAU + LBL A PI DIV PI RST.

Björn Gustavsson also has 3 routines:

- 1) OP 20 RCL 00 PAU RST LBL A CMs RST
- 2) LBL A PI OP 10 + PAU RST
- 3) PI OP 10 + PAU RST LBL A RST (faster than # 2)

Ralph Snyder, true to form, sent me a lot of solutions one day, to recant them the very next day. So, here go Ralph's two solutions:

- 1) PAU DIV LBL A + RST
- 2) PAU + LBL A DIV RST

Both solutions run continuously in error condition, so to stop them hold R/S down until the display winks. Then press CLR.

Erik Kempf in Denmark also put up a good show with these routines:

- 1) PAU SUM+ RST LBL A RST
- 2) PAU + CE DIV RST LBL A DIV CE + RST

Erik says that stopping the program results in flashing. But why stopping, he adds. My program is still running, so I will be forced to buy a new TI-59! He ends his letter with: Puzzling er sjovt! (puzzling is fun) to which I say to all of you: Ja, vi havde det vældig sjovt! (yes indeed, we have had lots of fun)

and appendix B contains the answers to problems.

The book is intended for first-year calculus students. It makes a unique use of the TI-59 and its programs to do virtually all the aspects of computation of the calculus.

I cannot think of any better and easier way to be introduced to calculus. I am jealous of the younger people having this wonderful and easy method to learn a rather involved subject. By using the programmable calculator you can have it do all the computational drudgery, while you are able to concentrate on the "meat" of the matter, learning calculus.

I highly recommend it to anyone wanting to learn or simply refresh calculus.

(Maurice Swinnen)

DIGIT REVERSER PUZZLE. - I received numerous solutions to this one I had attributed to

Harald M. Otto. I knew, of course, that Reinhold Patzer, a compatriot of Harald, had solved it in 52-Notes, v3n4p4. It was an improvement on one by Jared Weinberger (remember Jared from Bologna, Italy?) in v2n11p6. But I just hoped that nobody would remember it and those who did would not remember the source.

But you can always count on Patrick Acosta to have a mind as a steel trap. He remembered and reminded me of it. Patrick has a nice solution himself: $LBL E CMs CP - INV INT SUM 03 = DIV 10 PRD 03 = INV X=T 004 RCL 03 R/S$.

Joseph P. Hanson's solution is unconventional in that it starts with the number in R10 and leaves the inverted version in R11. The EE at step 030 is necessary; without it, summing exponential and non-exponential formats into R11 produces rounding errors. Joe's version may be found among many others on the next two pages.

John R. Adams tells me that his solution has the following characteristics:

1. Zero and single-digit numbers are reversed. (Hold onto that one, Jack. We can use it in our next April joke. Brilliant. Ed.)
2. Negative numbers are inverted and remain negative. (Some of the other solutions don't do that. Ed.)
3. For numbers greater than 1×10^{13} , all significant digits can be inverted if one ignores the exponent and is careful in how the 13 digits are retrieved.

HARALD M. OTTO
REINHOLD PATZER
West Germany

000	76	LBL
001	11	R
002	53	(
003	24	CE
004	55	+
005	01	1
006	00	0
007	49	PRD
008	01	01
009	75	-
010	22	INV
011	59	INT
012	44	SUM
013	01	01
014	54)
015	22	INV
016	67	EQ
017	11	R
018	53	(
019	48	EEC
020	01	01
021	65	X
022	01	1
023	00	0
024	54)
025	92	RTN

From Nello Coda you will find several solutions. The first one reverses the order for any number up to 13 digits, by pressing A the first time, R/S all subsequent times. The second one reverses a number with trailing zeros and yields the zeros again when re-reversed. The third routine preserves both leading and lagging zeros, provided the number of digits is entered first. For example, consider the 6-digit number 012300. Enter 6 and press A. Enter 012300 or simply 12300, because a leading zero doesn't show up in the display, and press R/S repeatedly. The numbers 3210 and 12300 will alternate with each R/S.

Now for Ralph Snyder: That "fussy old boy" (his own words) is always panting along with some amendments to his submissions: three tries for the Dimension Operations last summer, three and a half for his famous Internal Rate of Return, two separate entries for the Digit Reverser and a pair of amendments for something he calls Digit Reverser by Alphas. Well, out of sheer fear of making an error in the transcription and incurring his holy wrath again, even after my retirement as editor, I am showing you here the last one of each version, LITTERALLY, reduced so they would fit. Any error you find is Ralph's. Look him up in the Indianapolis telephone guide.

By the way, Don O'Grady, the author of many modules and also of the Master Library for the TI-88, told me recently, at the occasion of my visit to Lubbock to be trained on the 88, that he used Ralph's equations for the financial programs. It permitted a much faster solution to financial problems with fewer iterations and higher accuracy. This coming from Don is a real complement. Ralph would also have had his name immortalized in the Manual, if the 88 had flown.

Please find a compilation of the many routines I received on the next two pages. My sincere thanks to everybody who participated. It was real fun.

Digit Reverser Puzzle

DIGIT REVERSER. Ralph W. Snyder, Indianapolis.

9. A	13.	A	76655.	000	91 R/S	013	02	02	026	00	00
123456789. B	1122334455.	+	766554.	001	76 LBL	014	95	=	027	00	00
9.	0.667}	=	7665544.	002	12 B	015	32 X/T		028	05	05
98.	1122334456.	x	766554433.	003	99 PRT	016	43 RCL		029	91 R/S	
987.	1122334456.	x	7.66554432.	004	32 X/T	017	02	02	030	76 LBL	
9876.	1000.	=	7.6655443 10	005	32 X/T	018	65	x	031	11 A	
98765.	1.1223345 12	TRACE	7.6655443 11	006	65	019	01	1	032	47 CMS	
987654.	1.1223345 12	B	7.6655443 12	007	93	020	00	0	033	42 STD	
9876543.	7.		1000.	008	01	021	95	=	034	00 00	
98765432.	76.		766554432.	009	75	022	99 PRT		035	99 PRT	
987654321.	766.		766554432.	010	22 INV	023	42 STD		036	98 RDV	
			0.211]	011	59 INT	024	02	02	037	81 RST	
				012	44 SUM	025	97 DSZ				

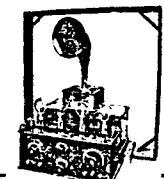
Instructions:

Numbers up to 10 digits: (1) Enter number of digits, press A. (2) Enter the number, press B. Reversal is printed by cumulative digits (for no printout delete PRT at Step 022; insert at Step 029 for printed answer).

Numbers exceeding 10 digits: (3) Enter number of digits, press A. (4) Enter first 10 digits, press +; enter remaining digits as a decimal, press = x; then, depending on whether the number has 11, 12 or 13 digits, enter a multiplier of 10, 100 or 1000, press = B. (For printout of this, press TRACE before entering digits, and again before pressing B.) (5) For an answer exceeding 10 digits, press TRACE +, then enter a divisor of 10, 100 or 1000 (matching the multiplier in operation (4)), and press = INV INT TRACE. The answer will be printed as 10 digits as an integer, and the remaining digits as a decimal. (See second example, showing printouts by operations (4) and (5).)



LEM HATTESON Kansas City, MO	JOSEPH P. HANSON Lexington MA	NELLO CODA Erie, PA	051 01 1 052 00 0 053 43 PRT 054 01 01 055 43 RCL 056 00 00 057 97 DSZ 058 02 02 059 14 D 060 43 PCL 061 01 01 062 91 R/S 063 22 INV 064 11 A 065 47 CMS 066 47 CP 067 81 RST	093 76 LBL 094 11 A 095 43 RCL 096 02 02 097 42 STD 098 01 01 099 59 INT 010 42 STD 011 44 SUM 012 00 00 013 44 SUM 014 01 01 015 01 01 016 00 0 017 49 PRT 018 00 0 019 43 RCL 020 00 00 021 02 02 022 22 INV 023 22 INV 024 01 01 025 01 01 026 01 01 027 01 01 028 01 01 029 32 X/T 030 43 RCL 031 02 02 032 47 CMS 033 42 STD 034 02 02 035 32 X/T 036 76 LBL 037 14 D 038 00 00 039 01 1 040 00 0 041 95 = 042 42 STD 043 00 00 044 22 INV 045 59 INT 046 22 INV 047 44 SUM 048 00 00 049 44 SUM 050 01 01	041 61 GTO 042 13 C 043 76 LBL 044 14 D 045 97 DSZ 046 02 02 047 13 C 048 43 RCL 049 01 01 050 91 R/S 051 76 LBL 052 11 A 053 47 CMS 054 29 CP 055 81 RST	JOHN ADAMS Pittsburg PA
			000 76 LBL 001 11 A 002 32 X/T 003 42 STD 004 42 STD 005 54 006 12 12 007 99 PRT 008 28 LDG 009 59 INT 010 42 STD 011 00 00 012 69 UP 013 20 20 014 76 LBL 015 16 R ¹ 016 43 RCL 017 11 11 018 55 019 01 1 020 00 0 021 75 022 59 INT 023 42 STD 024 11 11 025 95 026 42 STD 027 10 10 028 01 1 029 00 0 030 49 PRT 031 13 13 032 43 RLL 033 10 10 034 44 SUM 035 13 13 036 97 DSZ 037 00 00 038 16 R ¹ 039 01 1 040 00 0 041 49 PRT 042 13 13 043 43 RCL 044 13 13 045 99 PRT 046 98 RDV 047 91 R/S	000 76 LBL 001 11 A 002 32 X/T 003 42 STD 004 29 CP 005 97 DSZ 006 02 02 007 59 INT 008 76 LBL 009 11 A 010 43 RCL 011 44 SUM 012 00 00 013 44 SUM 014 01 01 015 01 01 016 00 0 017 49 PRT 018 00 0 019 53 020 24 CE 021 85 022 01 1 023 00 0 024 65 025 43 RCL 026 02 02 027 54 028 42 STD 029 02 02 030 00 0 031 95 032 22 INV 033 75 034 53 035 01 1 036 00 0 037 43 RCL 038 22 INV 039 00 0 040 22 INV 041 44 SUM 042 00 00 043 44 SUM 044 01 01 045 01 01 046 00 0 047 00 0 048 00 00 049 01 01 050 01 01	000 76 LBL 001 11 A 002 32 X/T 003 42 STD 004 29 CP 005 97 DSZ 006 02 02 007 59 INT 008 76 LBL 009 11 A 010 43 RCL 011 44 SUM 012 00 00 013 44 SUM 014 01 01 015 01 01 016 00 0 017 49 PRT 018 00 0 019 53 020 24 CE 021 85 022 01 1 023 00 0 024 65 025 43 RCL 026 02 02 027 54 028 42 STD 029 02 02 030 00 0 031 95 032 22 INV 033 75 034 53 035 01 1 036 00 0 037 43 RCL 038 22 INV 039 00 0 040 22 INV 041 44 SUM 042 00 00 043 44 SUM 044 01 01 045 01 01 046 00 0 047 00 0 048 00 00 049 01 01 050 01 01	000 76 LBL 001 11 A 002 32 X/T 003 42 STD 004 29 CP 005 97 DSZ 006 02 02 007 59 INT 008 76 LBL 009 11 A 010 43 RCL 011 44 SUM 012 00 00 013 44 SUM 014 01 01 015 01 01 016 00 0 017 49 PRT 018 00 0 019 53 020 24 CE 021 85 022 01 1 023 00 0 024 65 025 43 RCL 026 02 02 027 54 028 42 STD 029 02 02 030 00 0 031 95 032 22 INV 033 75 034 53 035 01 1 036 00 0 037 43 RCL 038 22 INV 039 00 0 040 22 INV 041 44 SUM 042 00 00 043 44 SUM 044 01 01 045 01 01 046 00 0 047 00 0 048 00 00 049 01 01 050 01 01
			009 01 01 010 00 00 011 00 00 012 00 00 013 00 00 014 00 00 015 00 00 016 00 00 017 00 00 018 00 00 019 00 00 020 00 00 021 00 00 022 00 00 023 00 00 024 00 00 025 00 00 026 00 00 027 00 00 028 00 00 029 00 00 030 00 00 031 00 00 032 00 00 033 00 00 034 00 00 035 00 00 036 00 00 037 00 00 038 00 00 039 00 00 040 00 00 041 00 00 042 00 00 043 00 00 044 00 00 045 00 00 046 00 00 047 00 00 048 00 00 049 00 00 050 00 00	009 01 01 010 00 00 011 00 00 012 00 00 013 00 00 014 00 00 015 00 00 016 00 00 017 00 00 018 00 00 019 00 00 020 00 00 021 00 00 022 00 00 023 00 00 024 00 00 025 00 00 026 00 00 027 00 00 028 00 00 029 00 00 030 00 00 031 00 00 032 00 00 033 00 00 034 00 00 035 00 00 036 00 00 037 00 00 038 00 00 039 00 00 040 00 00 041 00 00 042 00 00 043 00 00 044 00 00 045 00 00 046 00 00 047 00 00 048 00 00 049 00 00 050 00 00	009 01 01 010 00 00 011 00 00 012 00 00 013 00 00 014 00 00 015 00 00 016 00 00 017 00 00 018 00 00 019 00 00 020 00 00 021 00 00 022 00 00 023 00 00 024 00 00 025 00 00 026 00 00 027 00 00 028 00 00 029 00 00 030 00 00 031 00 00 032 00 00 033 00 00 034 00 00 035 00 00 036 00 00 037 00 00 038 00 00 039 00 00 040 00 00 041 00 00 042 00 00 043 00 00 044 00 00 045 00 00 046 00 00 047 00 00 048 00 00 049 00 00 050 00 00	009 01 01 010 00 00 011 00 00 012 00 00 013 00 00 014 00 00 015 00 00 016 00 00 017 00 00 018 00 00 019 00 00 020 00 00 021 00 00 022 00 00 023 00 00 024 00 00 025 00 00 026 00 00 027 00 00 028 00 00 029 00 00 030 00 00 031 00 00 032 00 00 033 00 00 034 00 00 035 00 00 036 00 00 037 00 00 038 00 00 039 00 00 040 00 00 041 00 00 042 00 00 043 00 00 044 00 00 045 00 00 046 00 00 047 00 00 048 00 00 049 00 00 050 00 00



Pretty sunny, cool;
chance of rain tomorrow!

DIGIT REVERSER BY ALPHAS. Ralph W. Snyder, Indianapolis.

5.	000 31 R/S	018 03 03 036 09 09 =	054 69 OP	072 69 OP	090 00 00
203040506.	001 69 OP	019 99 PRT	037 95 =	055 29 29	073 02 02 091 24 24
707091200.	002 00 00	020 69 OP	038 65 X	056 87 IFF	074 22 INV
0.	003 42 STD	021 05 05 039	01 1 057 =	01 01 075	086 STP
123456789	004 01 01	022 69 OP	040 00 00	058 00 00	076 01 01 094 11 R
987654321	005 69 OP	023 00 00	041 00 00	059 72 72	077 86 STP
	006 01 01	024 73 R/C*	042 95 =	060 87 IFF	078 02 02 096 05 5
	007 99 PRT	025 08 08	043 72 ST*	061 02 02	079 87 IFF
	008 91 R/S	026 65 X	044 09 09	062 00 00	080 02 02 098 42 STD
	009 42 STD	027 93 .	045 97 DS2	063 83 83	081 00 00 00 00
5.	202030304.	010 02 02	028 00 00	046 00 00	064 69 OP
405050606.	011 69 OP	029 01 1	047 00 00	065 01 01	080 69 OP
707080809.	012 02 02	030 75 -	048 - 24	066 86 STP	084 03 03 102 08 08
112233445566778	013 99 PRT	031 53 INT	049 05 5	067 01 01	085 69 OP
87766554433211	014 31 R/S	032 72 ST*	050 42 STD	068 87 IFF	086 05 05 104 42 STD
	015 42 STD	033 08 08	051 00 00	069 01 01	087 25 CLR
	016 03 03	034 85 +	052 73 R/C*	070 00 00	088 37 DSZ
	017 69 OP	035 73 R/C*	053 09 09	071 87 87	089 08 08 107 31 RST

Instructions.

(1) Press A. This sets two DSZ controls, one for the Digit Reversal "short loop" ending at Step 048, and the other for the "long loop" ending at Step 091 controlling the looping for the three alpha banks.

(2)(a) Enter the 1st alpha bank double-digits for the 1st 5 actual digits of the actual number. Press R/S.

(b) Same for 2nd alpha bank. Press R/S.

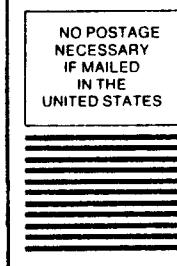
(c) Same for 3rd alpha bank (if there are no actual digits for any bank, enter 0). Press R/S.

Execution time from last R/S, about 23 seconds (about 21 seconds if no digits in 3rd bank).

Notes: Be sure to complete the full 10 alpha double-digits, using sufficient double zeros (00) to fill each bank; and remember that when entering say 02 for the actual digit 1 as the leading digits in any bank, the 0 is "silent" and need not be entered (if a leading 02 is keyed in, only 2 appears in the display and in the printout).

Remember that the digits 0 to 8 are entered in alpha by a zero followed by the actual digit-plus 1 (e.g., 0 is 01, 1 is 02, etc., and 8 is 09). The actual digit 9 is entered as 12.

JAMES BAUER Kenosha WI	053 55 +	JOHN HAMLIN Beaverton OR	051 00 0	000 76 LBL	D.RISTANOVIC Yugoslavia	014 01 1
000 76 LBL	054 01 1	052 85 +	001 11 A	015 00 0	015 00 0	016 49 PRD
001 11 A	055 00 0	053 69 OP	002 29 CP	000 76 LBL	017 01 01	017 01 01
002 47 CMS	056 45 YX	003 76 LBL	054 20 20	003 55 +	001 11 A	018 43 RCL
003 42 STD	057 43 RCL	004 11 A	055 43 RCL	004 53 <	002 42 STD	019 00 00
004 00 00	058 04 04	005 42 STD	056 16 16	005 28 LOG	003 00 00	020 59 INT
005 32 XIT	059 95 =	006 15 15	057 38 INT	006 59 INT	004 00 00	021 22 INV
006 01 1	060 91 R/S	007 28 LOG	058 40 RCL	007 65 +	005 01 1	022 67 EQ
007 03 3		008 59 INT	059 00 00	008 01 1	006 00 0	023 00 00
008 42 STD		009 85 +	060 22 INV	009 54 >	007 49 PRD	024 04 04
009 01 01		010 01 1	061 77 GE	010 22 INV	008 01 01	025 43 RCL
010 32 XIT		011 95 =	062 43 RCL	011 28 LOG	009 05 -	026 01 01
011 55 +		012 42 STD	063 73 R/C*	012 52 EE	010 49 PRD	027 01 R/S
012 01 1		013 00 00	064 00 100	013 22 INV	011 49 INT	
013 00 0		014 42 STD	065 95 =	014 52 EE	012 42 STD	
014 95 =		015 16 16	066 92 RTN	015 42 STD	013 00 00	
015 42 STD		016 43 RCL		016 00 00	014 65 X	
016 02 02		017 15 15		017 75 -	015 01 1	
017 22 INV		018 55 +		018 59 INT	016 00 0	
018 59 INT		019 40 RCL		019 44 SUM	017 95 =	
019 29 CP		020 00 00		020 01 01	018 44 SUM	
020 22 INV		021 28 LOG		021 95 =	019 01 01	
021 67 EQ		022 52 EE		022 65 X	020 43 RCL	HENRIK KLEIN Denmark
022 00 00		023 22 INV		023 00 00	021 00 00	
023 31 31		024 95 =		024 67 E9	022 22 INV	
024 65 X		025 76 LBL		025 49 PRD	023 67 EQ	023 76 LBL
025 01 1		026 59 CP		027 01 01	024 00 00	024 11 A
026 44 SUM		027 92 XIT		027 95 =	025 04 04	025 42 STD
027 04 04		028 48 RCL		028 22 INV	026 48 EXC	026 01 01
028 61 GTO		029 53 <		029 67 E9	027 01 01	027 76 LBL
029 00 00		030 32 XIT		030 00 00	028 91 R/S	028 16 R*
030 35 35		031 95 =		031 17 17		029 32 INV
031 85 +		032 95 =		032 48 EXC		030 59 INT
032 00 0		033 72 ST*		033 00 00	031 04 04	031 22 INV
033 49 PRD		034 00 00		034 00 00	032 22 INV	
034 04 04		035 00 00		035 49 PRD	033 01 01	
035 95 =		036 00 00		036 01 01	034 00 00	
036 65 X		037 00 00		037 44 SUM	035 25 CLR	
037 01 1		038 00 00		038 00 00	036 48 EXC	
038 00 0		039 00 00		039 00 00	037 01 01	
039 49 PRD		040 95 =		040 92 RTN	038 00 00	
040 03 03		041 65 X			039 04 04	
041 95 =		042 00 00			040 22 INV	
042 44 SUM		043 00 00			041 67 EQ	
043 03 03		044 00 00			042 55 +	
044 43 RCL		045 00 00			043 49 PRD	
045 02 02		046 76 LBL			044 01 01	
046 59 INT		047 67 EQ			045 01 01	
047 97 DSZ		048 73 R/C*			046 00 00	
048 01 01		049 00 00			047 00 00	
049 00 00		050 95 =			048 48 EXC	
050 11 11		051 65 X			049 00 00	
051 43 RCL		052 00 03			050 92 RTN	
052 03 03		053 01 1				



PIE CHARTS.- I once called Robert Prins from De Bilt, in the Netherlands, a master programmer. This was in a letter to the organizer of Procal meetings, a get-together of calculator fanatics in that country, Dr. Frans Van den Bogaard. Frans got that message back to Robert and ever since they have noticed a light swelling of young Robert's head accompanied by a noticeable elevating of the nose. And rightly so: In my eyes this young student at the Delft Technical University is one of the practitioners of the art of computing on small machines that has shown a rare insight into how these machines really work and has consistently come up with ingenious and practical programs. So, again he rose to the challenge I put up in one of the former issues and he sends me a program that will produce pie charts in double mode: Graphics and Fast modes. The Graphics part is a slight modification of Michael Sperber's Plot 60 using the STF h12 Fast mode entry with a smartly chosen initialization constant of " $1 \sqrt{x} x^2$ $1/x$ ", which sets only flag 4, so that you can start Fast mode by calling B and "pop" out into Normal mode by a RTN, without going into Trace mode after the RTN. This method was described by Patrick Acosta in v6n8p4.

The program is divided into 4 sections:
 Section 1: steps 000 through 239, the main section, needed for initialization, both Graphics and Fast mode.
 Section 2: steps 240 through 476, the "rotate and print" descriptor section.
 Section 3: steps 240 through 479, the first part of the actual pie printer.
 Section 4: steps 480 through 623, the rest of the pie printer.

Keying in the program:

- 1) Repartition to 4 OP 17 and key in listing 1, steps 000 through 239, followed by steps 240 through 479, and lastly steps 480 through 623. Record only bank 2 in this partitioning, i.e. 4 OP 17. Mark this track "2.1". Then reparation to 6 OP 17 and record banks 1 and 3 on a separate card.
- 2) Repartition again to 4 OP 17 and key in steps 240 through 476. Record this also as bank 2 on the remaining track of the very first card. Mark this track however "2.2".

You now must have two mag cards: one

with a bank 2 recorded on each track, marked 2.1 and 2.2 respectively and recorded in 4 OP 17 and a second mag card with banks 1 and 3 on it, recorded in 6 OP 17.

USING THE SYSTEM:

1. Make sure the Master Library module is in place.
2. Enter banks 1 and 3 in the calculator. (the 6 OP 17 card).
3. Create the two necessary hex codes: press from the keyboard: 10 OP 17 CLR GTO 016 PGM 19 SBR 045 P/R LRN INS (this creates h25) SST sixteen times, INS (this creates the h12) LRN RST CLR.
4. Enter the number of tapes wanted. I would start modestly with 1 or 2, and press A. The display will show a zero.
5. Enter the number of pie sectors you want. It has to be equal to or smaller than 20. Press R/S.
6. Enter the print code for the first sector of the pie chart and press the X:T key.
7. Enter the percentage for that first pie sector and press R/S.
8. Repeat steps 6 and 7 for all the pie sectors you want.

NOTE that percentages will be rounded to the nearest .5% and that they are stored, together with their print codes in R20, R20+n-1....where n is the number of slices. The percentage of each slice is added to all the previous ones. For matters of convenience the program works in GRAD mode (finally somebody outside France has found a use for the GRAD mode) because multiplying by 4 is easier than by 3.6 or pi/50.

After all the percentages have been entered, the display will show 2.1, meaning it wants the bank marked "2.1". DON'T TOUCH ANY KEY, just slide in the requested card, correct bank. However, if you happen to slide in bank 2.2, no harm is done. Each bank has its own ID number, and sliding in the wrong one will only cause the program to jump back to the entry point. That means 2.1 will appear again in the display. After entering 2.1, the program will still continue automatically, as it still is in Fast mode.

If you entered bank 2.2 correctly, it will check all entered angles i.e. percentages, for "legallity." Angles from 90 through 110 and from 290 through 310 are considered "illegal", as the would

cause Plot 60 to print nearly horizontal lines! When such an angle is encountered, all angles are rotated by 2% and tested again. If after 50 rotations, that is a 100% rotation, there are still illegal angles, the program will halt with a flashing 1/0.

If you want to alter this feature: steps 258-260 contain 050 (the max # of rotations) and steps 276-277, both of bank 2.1, contain 08, the rotation in grads.

After checking all rotations, the program prints out a list of names, percentages and identifiers, A through T.

After completion of this list, the display shows 2.2; enter bank 2.2 and sit back and enjoy; you will have about an hour to, according to Harald M.Otto, "drink a cup of the strong brew, smoke'm if you have'm and maybe you suddenly discover again you have been married for some time now..."

Now, suppose the printing is ready and you observe that it is either too large or too small to your taste. A Scottsman would say here: "Nay bodder at all." Just enter a new number of tapes and press A. The display will show 2.1,

for you to slide in card-bank 2.1. And, here shows the true genious of the pro-grammer, the program will now simply skip the rotation part and start right away with the print part. After printing of the list, the display will show again 2.2, indicating to slide in bank 2.2; do it and again you may sit back and continue doing whatever you were, before you were so rudily interrupted by this the halting of this insolent program!!!

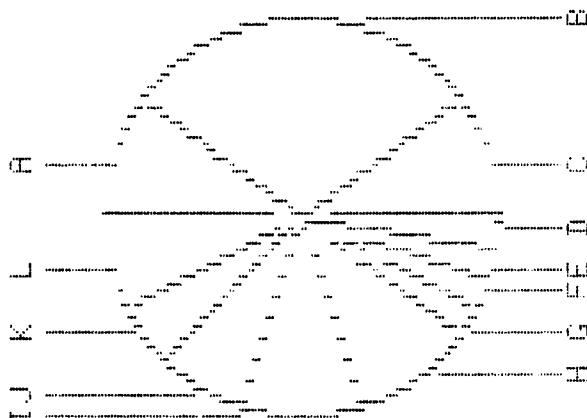
To print a brand new pie chart, always press RST before entering the number of tapes and pressing A.

At this point Robert gives a detailed explanation as to how the program exactly works. And in spite of his rather stern admonition to publish EVERYTHING or nothing at all, lest the user will not understand at all what is going on, I am going to risk incurring his wrath and leaving the explanation in its ori-ginal form, written on paper. If some of the fanatics want a copy of it, though, one can be had of this 22-page epistle (small wonder Swinnen left it out of the Notes) for \$4.00 US. By means of a yel-low filter it should be possible to ren-der a legible Xerox(TM) copy of this blue roll ball pen writing.

```

N N N N N N N N N N
O O O O O O O O O O
d d d d d d d d d d
M M M M M M M M M M
1 2 3 4 5 6 7 8 9 0
O O O O O O O O O O
O O O O O O O O O O
X X X X X X X X X X
A A A A A A A A A A
E E O A W L U H D Z U

```



See programs on next two pages.

CIRKELDIAGRAM,- As you might have guessed, that is Swedish for Pie Chart.(why not?)
----- Lars Nilsson, who obviously hails from that country, has also written a Fast Mode program to solve the Pie Chart problem. It works just fine but, unfortu-nately, there is not enough space in this issue to put in both solutions I received so far. I am sending Lars' program to Palmer Hanson, so that he may publish it even-tually in one of the future issues.

Pie Chart, Robert Prins.

000	92	RTH	076	49	PRD	152	02	02	228	02	02	304	23	23	380	85	+
001	76	LBL	077	02	02	153	40	40	229	44	SUM	305	29	CP	381	73	RC*
002	11	A	078	49	PRD	154	02	2	230	01	01	306	53	<	382	03	03
003	61	GTO	079	04	04	155	93	.	231	98	ADV	307	43	RCL	383	54	>
004	00	00	080	01	1	156	01	1	232	97	DSZ	308	05	05	384	42	STD
005	40	40	081	05	5	157	91	R/S	233	08	08	309	65	X	385	17	17
006	76	LBL	082	06	6	158	56	DEL	234	01	01	310	73	RC*	386	39	CDS
007	12	B	083	42	STD	159	56	DEL	235	75	75	311	03	03	387	67	EQ
008	61	GTO	084	14	14	160	92	RTN	236	00	0	312	59	INT	388	04	04
009	00	00	085	87	IFF	161	02	2	237	98	ADV	313	39	CDS	389	00	00
010	18	18	086	04	04	162	93	.	238	98	ADV	314	54	>	390	53	<
011	76	LBL	087	01	01	163	02	2	239	92	RTN	315	77	GE	391	46	INS
012	13	C	088	46	46	164	91	R/S	240	89	1	316	40	IND	392	65	X
013	25	CLR	089	00	0	165	92	RTN	241	32	X:T	317	15	15	393	43	RCL
014	69	DP	090	92	RTN	166	12	B	242	43	RCL	318	53	<	394	05	05
015	05	05	091	42	STD	167	61	GTO	243	07	07	319	43	RCL	395	54	>
016	74	SM*	092	16	16	168	02	02	244	22	INV	320	05	05	396	77	GE
017	90	90	093	42	STD	169	40	40	245	67	EQ	321	65	X	397	40	IND
018	12	B	094	18	18	170	02	2	246	01	01	322	73	RC*	398	15	15
019	20	CLR	095	01	1	171	05	5	247	52	52	323	03	03	399	22	INV
020	30	TAN	096	09	9	172	01	1	248	61	GTO	324	59	INT	400	86	STF
021	30	TAN	097	42	STD	173	42	STD	249	01	01	325	30	TRN	401	03	03
022	61	GTO	098	00	00	174	14	14	250	70	70	326	54	>	402	53	<
023	-53	<	099	53	<	175	09	9	251	86	STF	327	94	+/-	403	01	1
024	32	X:T	100	43	RCL	176	94	+/-	252	40	IND	328	53	<	404	75	-
025	93	.	101	00	00	177	42	STD	253	07	07	329	42	STD	405	43	RCL
026	01	1	102	75	-	178	05	05	254	87	IFF	330	17	17	406	05	05
027	34	FX	103	01	1	179	01	1	255	01	01	331	33	X:	407	33	X:
028	33	X:	104	09	9	180	12	B	256	03	03	332	85	+	408	75	-
029	35	1/X	105	54	>	181	69	DP	257	53	53	333	43	RCL	409	43	RCL
030	86	STF	106	29	CP	182	05	05	258	87	IFF	334	05	05	410	17	17
031	71	71	107	92	RTN	183	02	2	259	02	02	335	33	X:	411	38	SIN
032	35	1/X	108	53	<	184	12	B	260	03	03	336	75	-	412	42	STD
033	43	RCL	109	46	INS	185	13	C	261	53	53	337	01	1	413	17	17
034	03	03	110	65	X	186	97	DSZ	262	02	2	338	54	>	414	33	X:
035	97	DSZ	111	02	2	187	05	05	263	08	8	339	77	GE	415	54	>
036	74	74	112	85	+	188	01	01	264	00	0	340	40	IND	416	77	GE
037	72	ST*	113	93	.	189	85	85	265	42	STD	341	15	15	417	40	IND
038	00	0	114	05	5	190	69	DP	266	15	15	342	43	RCL	418	15	15
039	04	4	115	54	>	191	35	35	267	53	<	343	17	17	419	22	INV
040	69	DP	116	53	<	192	43	RCL	268	01	1	344	61	GTO	420	87	IFF
041	17	17	117	59	INT	193	06	06	269	75	-	345	04	04	421	03	03
042	87	IFF	118	65	X	194	42	STD	270	43	RCL	346	72	72	422	04	04
043	04	04	119	02	2	195	00	00	271	05	05	347	97	DSZ	423	39	39
044	00	00	120	85	+	196	00	0	272	33	X:	348	18	18	424	53	<
045	49	49	121	73	RC*	197	12	B	273	54	>	349	03	03	425	43	RCL
046	47	CMS	122	00	00	198	13	C	274	34	FX	350	03	03	426	17	17
047	01	1	123	59	INT	199	43	RCL	275	42	STD	351	86	STF	427	69	DP
048	93	.	124	85	+	200	04	04	276	17	17	352	02	02	428	10	10
049	00	0	125	32	X:T	201	44	SUM	277	61	GTO	353	04	4	429	75	-
050	05	5	126	55	+	202	05	05	278	04	04	354	04	4	430	43	RCL
051	94	+/-	127	01	1	203	97	DSZ	279	72	72	355	07	7	431	05	05
052	42	STD	128	00	0	204	00	00	280	01	1	356	42	STD	432	69	DP
053	01	01	129	22	INV	205	01	01	281	00	0	357	15	15	433	10	10
054	02	2	130	28	LOG	206	96	96	282	44	SUM	358	43	RCL	434	54	>
055	93	.	131	54	>	207	09	9	283	15	15	359	16	16	435	22	INV
056	01	1	132	69	DP	208	42	STD	284	43	RCL	360	42	STD	436	67	EQ
057	42	STD	133	20	20	209	05	05	285	17	17	361	18	18	437	40	IND
058	02	02	134	72	ST*	210	02	2	286	94	+/-	362	01	1	438	15	10
059	03	3	135	00	00	211	12	B	287	61	GTO	363	09	9	439	05	5
060	00	0	136	97	DSZ	212	13	C	288	04	04	364	42	STD	440	04	4
061	35	1/X	137	18	18	213	97	DSZ	289	72	72	365	03	03	441	07	7
062	42	STD	138	01	01	214	05	05	290	05	5	366	80	GRD	442	48	EXC
063	04	04	139	01	01	215	02	02	291	07	7	367	53	<	443	17	17
064	06	6	140	02	2	216	12	12	292	44	SUM	368	93	.	444	61	GTO
065	00	0	141	05	5	217	69	DP	293	15	15	369	05	5	445	04	04
066	42	STD	142	08	8	218	00	00	294	43	RCL	370	65	X	446	72	72
067	06	06	143	93	.	219	13	C	295	16	16	371	53	<	447	97	DSZ
068	32	X:T	144	02	2	220	02	2	296	42	STD	372	73	RC*	448	18	18
069	42	STD	145	06	6	221	42	STD	297	18	18	373	03	03	449	03	03
070	08	08	146	07	7	222	05	05	298	01	1	374	75	-	450	67	67
071	49	PRD	147	93	.	223	01	1	299	09	9	375	69	DP	451	00	0
072	06	06	148	02	2	224	12	B	300	42	STD	376	23	23	452	48	EXC
073	69	DP	149	06	6	225	69	DP	301	03	03	377	73	RC*	453	09	09
074	26	26	150	12	B	226	05	05	302	80	GRD	378	03	03	454	69	DP
075	35	1/X	151	61	GTO	227	43	RCL	303	69	DP	379	54	>	455	01	01

Pie Chart, Robert Prins.

456	00	0	532	32	XIT	608	59	INT	252	07	07	327	03	03	403	57	ENG
457	48	EXC	533	02	2	609	65	x	253	43	RCL	328	15	15	404	85	+
458	10	10	534	32	INV	610	03	3	254	07	07	329	43	RCL	405	93	.
459	69	DP	535	67	EQ	611	85	+	255	61	GTO	330	16	16	406	04	4
460	02	02	536	05	05	612	53	<	256	01	01	331	42	STD	407	85	+
461	00	0	537	44	44	613	46	INS	257	66	66	332	18	18	408	00	0
462	48	EXC	538	02	2	614	55	+	258	00	0	333	01	1	409	48	EXC
463	11	11	539	05	5	615	03	3	259	05	5	334	09	9	410	05	05
464	69	DP	540	93	.	616	00	0	260	00	0	335	42	STD	411	54	>
465	03	03	541	02	2	617	54)	261	42	STD	336	03	03	412	65	x
466	00	0	542	07	7	618	59	INT	262	17	17	337	00	0	413	04	4
467	48	EXC	543	93	.	619	65	x	263	02	2	338	42	STD	414	22	INV
468	12	12	544	04	4	620	02	2	264	09	9	339	05	05	415	28	LOG
469	69	DP	545	07	7	621	54)	265	04	4	340	53	<	416	54	>
470	04	04	546	59	INT	622	83	GD*	266	93	.	341	53	<	417	69	DP
471	92	RTN	547	52	EE	623	17	17	267	03	3	342	53	<	418	03	03
472	53	<	548	94	+/-				268	02	2	343	73	RCL	419	01	1
473	53	<	549	44	SUM				269	09	9	344	03	03	420	01	1
474	46	INS	550	13	13				270	42	STD	345	59	INT	421	09	9
475	75	-	551	53	<				271	14	14	346	94	+/-	422	33	X^
476	43	RCL	552	73	RCL*				272	12	B	347	85	+	423	82	HIR
477	01	01	553	13	13				273	61	GTO	348	69	DP	424	08	08
478	54	>	554	55	+				274	01	01	349	23	23	425	53	<
479	55	+	555	43	RCL				275	66	66	350	73	RCL*	426	73	RCL*
480	01	1	556	07	07				276	00	0	351	03	03	427	03	03
481	32	XIT	557	22	INV				277	08	8	352	59	INT	428	85	+
482	43	RCL	558	28	LOG				278	74	SM*	353	85	+	429	01	1
483	02	02	559	33	X^				279	07	07	354	93	.	430	00	0
484	54	>	560	52	EE				280	69	DP	355	04	4	431	00	0
485	77	GE	561	22	INV				281	27	27	356	54	>	432	54	>
486	40	IND	562	57	ENG				282	97	D92	357	55	+	433	82	HIR
487	15	15	563	42	STD				283	03	03	358	04	4	434	06	06
488	29	CP	564	07	07				284	02	02	359	54	>	435	04	4
489	22	INV	565	54)				285	78	78	360	52	EE	436	05	5
490	77	GE	566	53	<				286	97	D92	361	55	+	437	03	3
491	40	IND	567	22	INV				287	17	17	362	52	EE	438	42	STD
492	15	15	568	59	INT				288	02	02	363	00	0	439	17	17
493	53	<	569	65	x				289	99	99	364	01	1	440	53	<
494	53	<	570	01	1				290	00	0	365	94	+/-	441	43	RCL
495	53	<	571	00	0				291	35	1/X	366	42	STD	442	03	03
496	46	INS	572	00	0				292	66	PAU	367	17	17	443	75	-
497	65	x	573	54)				293	81	RST	368	54	>	444	06	6
498	04	4	574	59	INT				294	93	.	369	28	LOG	445	93	.
499	85	+	575	29	CP				295	09	9	370	48	EXC	446	03	3
500	09	9	576	22	INV				296	09	9	371	17	17	447	08	8
501	75	-	577	67	EQ				297	32	XIT	372	53	<	448	54	>
502	59	INT	578	40	IND				298	80	GRD	373	53	<	449	53	<
503	42	STD	579	15	15				299	01	1	374	53	<	450	61	GTO
504	13	13	580	53	<				300	09	9	375	46	INS	451	05	05
505	54	>	581	43	RCL				301	42	STD	376	65	x	452	99	99
506	65	x	582	07	07				302	00	00	377	01	1	453	65	x
507	05	5	583	65	x				303	42	STD	378	00	0	454	04	4
508	42	STD	584	43	RCL				304	07	07	379	00	0	455	22	INV
509	07	07	585	13	13				305	53	<	380	49	PRB	456	28	LOG
510	85	+	586	22	INV				306	43	RCL	381	05	05	457	54	>
511	59	INT	587	59	INT				307	16	16	382	34	FX	458	69	DP
512	94	+/-	588	54)				308	85	+	383	85	+	459	01	01
513	44	SUM	589	74	SM*				309	01	1	384	01	1	460	69	DP
514	07	07	590	13	13				310	54)	385	85	+	461	05	05
515	54	>	591	83	GD*				311	42	STD	386	28	LOG	462	97	D82
516	65	x	592	15	15				312	05	05	387	59	INT	463	18	18
517	03	3	593	53	<				313	42	STD	388	65	x	464	03	03
518	54	>	594	43	RCL				314	03	03	389	02	2	465	40	40
519	52	EE	595	03	03				315	73	RCL*	390	75	-	466	69	DP
520	59	INT	596	75	-				316	00	00	391	59	INT	467	00	00
521	87	IFF	597	07	7				317	59	INT	392	44	SUM	468	69	DP
522	01	01	598	54)				318	38	SIN	393	05	05	469	05	05
523	05	05	599	53	<				319	50	IIXI	394	54	>	470	01	1
524	93	93	600	46	INS				320	77	GE	395	97	D92	471	06	6
525	87	IFF	601	85	+				321	02	02	396	17	17	472	01	1
526	02	02	602	53	<				322	76	76	397	03	03	473	42	STD
527	05	05	603	46	INS				323	69	DP	398	74	74	474	14	14
528	44	44	604	55	+				324	20	20	399	52	EE	475	89	#
529	67	E0	605	01	1				325	97	D92	400	00	0	476	92	RTN
530	05	05	606	08	8				326	05	05	401	04	4			
531	41	41	607	54)				327	22	INV	402					

INTEGRATION, HENRIK KLEIN, DENMARK

TI 59 INTEGRATION
This is a pocket of programs designed to solve most problems encountered in numerical integration. It consists of a main program which can handle most functions, supplemented with two secondary programs used in special cases.

THEORY

When the following is true for an integrable with the exact value I :

$$I = T(h) + Ah^q + Bh^{2q} + \dots \quad (1.1)$$

where $T(h)$ is an approximation to I and h is the width of the intervals used ($h = (b-a)/n$), then h may be chosen so small that Bh^q is much smaller than Ah^q which means that the following approximation can be done:

$$I \approx T(h) + Ah^q \quad (1.2)$$

If there in addition is another value based on $2h$:

$$I \approx T(2h) + A(2h)^q \quad (1.3)$$

then A may be eliminated from (1.2) and (1.3):

$$I \approx \frac{(2h)^q T(h) - h^q T(2h)}{2^q - 1} = T(h) + \frac{T(h) - T(2h)}{2^q - 1} \quad (1.4)$$

Used in (1.1) this yields:

$$I = T(2h) + Bh^{2q} + \dots \quad (1.5)$$

which means that the fault now is in the order of h^{2q} , i.e. smaller than before. These calculations is now the assumption that q is known. If this is not the case another approximate value of I , based on $4h$, is needed. This yields:

$$2^q = \frac{T(4h) - T(2h)}{T(2h)} \Leftrightarrow q = \frac{1}{\ln 2} \ln \left[\frac{T(4h)}{T(2h)} - 1 \right] \quad (1.6)$$

$$I = T(h) \frac{T(4h)}{T(2h)} - 2^q \frac{T(2h)}{T(h)} = T(h) - \frac{T(4h)}{T(2h)} + \frac{T(h)}{T(h)} \quad (1.7)$$

The above is called Aitken-extrapolation while (1.4) is called Richardson-extrapolation.

ROMBERG-INTEGRATION

When $f(x)$ and all of its derivatives are continuous in the whole integration interval a simple case of (1.1) results if either the trapez-formula or the center-formula is used to calculate approximate I -values:

$$I = T(h) + Ah^2 + Ah^4 + \dots + Ah^{2k} + \dots \quad (1.8)$$

Now the idea with Romberg-integration is that some $T(h)$ values are calculated for each new value. One basis of these new values are calculated with the use of (1.4), which means that the term with h^2 is eliminated. These new values are used to remove the term with h^4 . A general outline of this procedure is shown in fig 1. The first vertical column is calculated by using the trapez-formula, as mentioned earlier:

$$\begin{aligned} T_0 &= \frac{1}{2}(f(a) + f(b)) + h \sum_{n=1}^{n-1} f(a+sh) ; h = \frac{b-a}{n} , n = \{2,4,8,16,32,\dots\} \\ T_n &= \frac{h}{2}(f(a) + f(b)) + h \sum_{s=1}^{n-1} f(a+sh) \end{aligned}$$

The next columns are derived from the first by the use of (1.4). For example is T_1 derived from T_0 and T_2 . Instead of the trapez-formula the center-formula (if I do not know the english name, this is a direct translation of the danish name) may be used:

$$M_n^e = h \sum_{s=1}^{n-1} f(a+h(s-\frac{1}{2})) , \quad h = \frac{b-a}{n} , \quad n = \{1,2,4,8,16,\dots\}$$

Note: a and b refer respectively to the lower and upper limits of the integration interval, i.e. $I = \int_a^b f(x) dx$.

number of intervals	size of fault					no. of intervals	no. of extrapolations
	h^2	h^4	h^8	h^{16}	h^{32}		
1	T_0					1	T_1
2	T_0	T_1				2	T_2
4	T_0	T_1	T_2			4	T_3
8	T_0	T_1	T_2	T_3		8	T_4
16	T_0	T_1	T_2	T_3	T_4	16	T_5
32	$-$	$-$	$-$	$-$	$-$	32	T_6
$-$	$-$	$-$	$-$	$-$	$-$	$-$	$-$

Fig 1 showing structure of Romberg-integration

FOX-ROMBERG & AIKEN-INTEGRATION

When $f(x)$ and/or one of its derivatives have one or more points where the function is not defined the ordinary Romberg method does not work

$\int_a^b f(x) dx$

(1.1) looks like this:
 $I = T(h) + Ah^2 + Ah^4 + \dots + Ah^{2k} + \dots$

When using ordinary Romberg, the term with $h^{1.5}$ is not eliminated, and the convergence towards I goes very slow. The term with $h^{1.5}$ can however be eliminated with Richardson-extrapolation, using $Q = 1.5$.

The value of Q must be determined on the basis of approximate values calculated with the use of (1.6). The method of using modified Romberg-integration is called Fox-Romberg.

Another possibility is to use Aitken-extrapolation, i.e., (1.7). Then there is no need for determining Q -values, but on the other hand more $T(h)$ values are needed, and the convergence is consequently slower. Fig 2 shows the structure of Aitken-integration.

RECORDING INSTRUCTIONS

Using the turn-on partitioning, 6 Up 17, read in the main program consisting of programsteps 000-239 and registers 35-44. Record bank 1 and 3 on one meg card. Then read in the Aid program, programsteps 360-479, and record bank 2 on a new meg card.

OUTPUT WITHOUT PRINTER

If you do not have a printer, you may though it is not necessary, replace the print-instructions with [RTS] or [Pause]. There is print-instructions at step 075, 103 and 120. The Aid program must be modified by changing the print-instruction at step 418 or you will not get an output of the approximate Q -values.

USER-DEFINED KEYS

LBL A Enter the lower limit of the integral $\int_a^b f(x) dx$.

LBL B Enter the upper limit of the integral $\int_a^b f(x) dx$.

LBL C Enter c , that is the limit of error. If nothing is entered $c = 10^{-10}$ is used, which means that the output will have at least 10 correct digits.

LBL D Initialize for entering of extra Q -values. These values are entered with the use of [RTS] and 120.

LBL E Start the numerical integration using either Romberg or Fox-Romberg, programming-status. The trapez-formula is used.

LBL F Center the formula will automatic shift to the Aid program.

LBL G The center-formula is used.

LBL H As LBL E, but in addition approximate Q -values are calculated with the use of the Aid program.

INTEGRATION, HENRIK KLEIN, DENMARK

THE TRAPEZ- AND CENTER-FORMULA
As basis for the extrapolations you may choose between two methods: The center-formula and the trapez-formula. The last one is the fastest and is for that reason preferable, but at times it is necessary to use the center-formula.

When flag 0 is set, the center-formula is used. If not the trapez-formula is used. $\boxed{[F]}$ sets flag 0, while $\boxed{[C]}$ clears flag 0.

USER INSTRUCTIONS FOR ROMBERG INTEGRATION

Only bank 1 and 3 is needed when using ordinary Romberg. The function is entered from step 200 and forward. Simply press \boxed{A} and start to program the function. When the function is called the program is in the middle of a summation, so do not use any terminating operations. Finish with $\boxed{INV} \boxed{SBR} \boxed{LN}$. x is in the display (x-register) when $f(x)$ is called. Registers 45 through 59 may be used for the evaluation of the function.

The limit of error is entered by pressing \boxed{E} , if convenient \boxed{SET} . When nothing is entered, i.e. the t-register is zero, then $\epsilon = 10^{-10}$ is used, and the result will normally be with 10 correct digits. If the result is found with incorrect digits and more correct digits is wanted, you may press $\boxed{R75}$ and the program will continue from where it stopped and make an extra series of extrapolations. This may be repeated, but another possibility is to enter a new ϵ value, though this must take place with the use of \boxed{SET} .

As an example is used $\int_0^1 \frac{1}{x+1} dx = \ln 2 = 0.6931471806$ (10 correct digits)

Procedure: $\boxed{A} + 240 00, \boxed{[T] \boxed{EE} \boxed{+} 1 \boxed{[T] \boxed{x} \boxed{INV} \boxed{SBR} \boxed{LN}}$
 $\quad \boxed{0} \boxed{A} + q, 1 \boxed{B} + 1, .001 \boxed{T}, \boxed{E} + 0.6931746032$ (14 sec)
 $\quad 10 \boxed{+/-} \boxed{INU} \boxed{LOG} \boxed{KIE} \boxed{R75} + 0.6931471806$ (44 sec)

OUTPUT ON PRINTER

When a printer is attached when running the above example, the result will be as shown in fig 1. All the T-values shown in fig 1 is printed, one row at a time. This can be very useful when dealing with functions which doesn't behave normally.

ROMBERG INTEGRATION FAILS

As mentioned earlier the Romberg method sometimes fails. An example was

$\int_0^1 \sqrt{x} dx = \frac{2}{3} \times \frac{3}{2} = 0.2357022604$ (10 correct digits)

TRY WITH ORDINARY ROMBERG:

$\boxed{A} \boxed{[T] \boxed{INV} \boxed{SBR} \boxed{LN}} \boxed{0} \boxed{A} .5 \boxed{B} \boxed{E} + 0.2347001681$ (74 minute)

That is only 5 correct digits, where there is supposed to be 10. When ordinary Romberg takes exceptional long time to compute an integral, change to one of the secondary methods.

*See EXAMPLES for further explanation.

FOX-ROMBERG INTEGRATION

The problem when using Fox-Romberg is to determine the theoretical q-values on the basis of the approximate Q-values.

Continuing the above example, read in the aid program. This clears the entered function, which was in bank 2. If you forget to reenter the function, the program will automatically shift to programming status

You won't need to reenter the upper and lower limits, simply press \boxed{E} in order to get q-values. With printer attached you will get a printout as shown in fig 4. The upper index refer to the order (no. of extrapolations), while the lower refer to the highest number of intervals used to calculate the T-values. q is calculated by inserting T_1 and T_2 in (1.4) , while q_2 is based on T_1 and T_2 .

If $f(x)$ and its derivatives are continuous in the integration interval, then $q_0 = 2$, $q_1 = 6$, $q_2 = 6$ etc. (See theory). This is obviously not the case in fig 4, where all q-values approximately are equal to 0.5, which must be presumed being the theoretical q-value. This value is entered using the following procedure:

$\boxed{D} + 34, 1.5 \boxed{R75} + 1.828427125$ (eller 2.5 - 1)

Now the program is ready to do the actual Fox-Romberg integration, which may be started using either \boxed{E} or \boxed{SET} . Note: The aid program is only used for calculating approximate q-values together with T-values. If you know the q-value of a function, you naturally don't need the aid program.

In fig 5 is the printout using \boxed{E} shown. Now the q-values are as expected, i.e. 1.5, 2, 4, 6 etc. Notice that the extra q-value is represented. This will only take place when the q-value is smaller than 2; when the q-value is larger than 2, 2 will appear twice.

Sometimes it is necessary to use more than one extra q-value, as here:

$$\int_0^1 \sqrt{x+1/x} dx = 1.649915823 \quad (10 \text{ correct digits})$$

Now $f(x)$ is not defined for $x = 0$, as $f(x) \rightarrow \infty$ when $x \rightarrow 0$. Therefore it is a necessity to use Fox-Romberg. For the same reason it is impossible to use the trapez-formula as this uses the boundaries in the evaluation of T (try!). Instead the center-formula is used:

$\boxed{A} \boxed{[T] \boxed{+} \boxed{1} \boxed{X} \boxed{E} \boxed{SET} \boxed{LN} \boxed{0} \boxed{A} .5 \boxed{B} \boxed{E} \boxed{E}$

The theoretical q-value is determined to $q = 4$, which is entered:

$\boxed{D} + 34, .5 \boxed{R75} + .4142135624, \boxed{E}$

Now we can determine the q-value to $q = 1.5$. We now have two theoretical q-value which both have to be entered; the entered q-value from before is not preserved. The order in which the two values are entered is unimportant, but in order to get the most influential extrapolation done first, you may as a matter of form enter the largest first. When running the program, you'll get 10 correct digits. The execution time is quite long now, which is especially caused by the use of the center-formula, which is almost twice as slow as the trapez-formula.

REMARKS TO CLEAR ENTERED Q-VALUES BEFORE ACTIVATING TO COMPUTE ANOTHER INTEGRAL:
This can be done by pressing \boxed{SET} , or better still \boxed{RST} which clears all flags, and actually initialize the program.

You can enter a maximum of three extra q-values.
Both Romberg and Fox-Romberg have limited running time, as they can't go higher than T_{20} .
Suggestion for card-marking:

$\boxed{A} \boxed{[T] \boxed{INV} \boxed{SBR} \boxed{LN}}$	$\boxed{R75}$	\boxed{SET}
\boxed{a}	\boxed{b}	\boxed{c}
$\boxed{q_1 R75 + 1.5}$	$\boxed{q_2 R75 + 1.5}$	$\boxed{q_3 R75 + 1.5}$

IMPORTANT NOTES

REMARKS TO CLEAR ENTERED Q-VALUES BEFORE ACTIVATING TO COMPUTE ANOTHER INTEGRAL:
This can be done by pressing \boxed{SET} , or better still \boxed{RST} which clears all flags, and actually initialize the program.

If you have got the impression that these programs always works, you're wrong!
The following integrals seems to be a simple problem:

$\int_0^1 1/x dx = 1 \ln 10 = 2.302565093$

$\boxed{A} \boxed{[T] \boxed{INV} \boxed{SBR} \boxed{LN}} \boxed{1} \boxed{A} 10 \boxed{B} \boxed{E} + 2.302565096$ (24 minute)

That is only 9 correct digits, where there is supposed to be 10. All derivatives of $f(x)$ is continuous, so there is no extra q-value missing. I can't tell why the program fails, only point out how to overcome it.
The program compares T_1 with T_{10} in order to determine the size of the fault. The most correct method would be to compare T_1 with T_{11} , but this would in most cases prolong the execution-time unnecessarily.

Now, the program uses normally about 60 sec to compute an integral. If the execution-time is much longer than this, you should compare T_1 with T_{20} . In the above example that is T_6 and T_{10} . Look at the two or three last digits

INTEGRATION, HENRIK KLEIN, DENMARK

AITKEN INTEGRATION The program is as simple as ordinary Romberg. The program is an alternative to Fox-Romberg. This program is as simple as ordinary Romberg, and you won't have to mess about with extra q-values. On the other hand the program is proportionally slow.

Record bank on one meg card. There is no registers to record.

The user defined keys are as before, or current R00 and Lbl E which both are omitted. The printout resembles that of Romberg, except for an extra T-value every other time as shown in fig 2.

EXAMPLES

Try the following examples:

$$\begin{aligned} \int_0^1 \ln x \, dx &= 2 \quad * \quad q = 1 \\ f(x) &: \boxed{\text{1}} \boxed{\text{inx}} \boxed{+/-} \boxed{=} \boxed{1} \quad \boxed{1} \\ \int_0^1 x^{3/2} \, dx &= 0.4 \quad * \quad q = 2 \frac{1}{2} \\ f(x) &: \boxed{\text{1}} \boxed{\text{CE}} \boxed{x} \boxed{[x]} \quad \boxed{1} \end{aligned}$$

- SURVEY OF MAIN PROGRAM

Entering of a, b and c.
The address for indirect call of 2^{q-1} values is loaded in R01 and floc 2 is set.
Enter extra q-values, while adjusting the address in R01.
023-039 Enter extra q-values, while adjusting the address in R01.
040-047 If flag 0 is set, the center-formula is used.
048-054 If flag 1 is set, the old program is used.
055-059 If R01 is not made ready, then c 10-101 is entered.
060-079 If the t-register is zero, then c 10-101 is entered.
071-079 If R04 is cleared, the first T is calculated, while initializing both trapez- and the center-formula.
080-083 If flag 1 is set: shift to old program.
084-102 If flag 1 is set: series of extrapolations. A new T is calculated.
103-123 Extrapolation using (1.4)
124-146 The last T is loaded into the correct register, while determining the size of the fault.
147-178 Init of trapez/center-formula. In the case of the trapez-formula the first T is calculated.
179-187 If the trapez-formula is used: return to 076. otherwise R10 is cleared to init the center-formula. The reason for step 184 is to stop possible flashing display.

188-205 The width of the intervals is bisected, the number of intervals is doubled and the first x-value is determined.

206-217 The evaluation of f(x), which is summed into R10.

218-236 The numerical integration is finished. R10 is cleared if the center-formula is used. Notice the difference between the two methods: The trapez-formula uses the earlier found f(x)-values, while the center-formula starts all over each time.

The old program replaces 084-146 in the main program, and is generally similar to these, except the additional capability of calculating approximate q-values.

SURVEY OF REGISTERS

R00 DSZ counter for extrapolations
R01 DSZ counter for call of the first 2^{q-1} value.
R02 The address for call of 2^{q-1} values. Starting value equal to R01.
R03 Address for indirect storing of T-values.
R04 Counter for number of possible extrapolations. Used in R00
R05 DSZ-counter for trapez/center integration. Index in old program
R06-R07 $\frac{a+b}{2}$.
R08 Trapez-formula: n/2, center-formula: n (number of intervals)
R09 Trapez-formula: 2h, center-formula: h (width of intervals)
R10 $\sum_{i=1}^n f(x_i)$ R23 $T_n^1 - T_n^0$ (only aidprg) R32-34 For extra 2^{q-1}
R11 $R_n^1 - R_n^0$ R31 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R12 \vdots R32 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R13 \vdots R33 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R14 \vdots R34 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R15 \vdots R35 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R16 \vdots R36 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R17 \vdots R37 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R18 \vdots R38 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R19 \vdots R39 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R20 \vdots R40 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R21 \vdots R41 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R22 \vdots R42 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R23 \vdots R43 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R24 \vdots R44 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R25 \vdots R45 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R26 \vdots R46 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R27 \vdots R47 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R28 \vdots R48 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R29 \vdots R49 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R30 \vdots R50 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R31 \vdots R51 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R32 \vdots R52 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R33 \vdots R53 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R34 \vdots R54 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R35 \vdots R55 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R36 \vdots R56 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R37 \vdots R57 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R38 \vdots R58 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R39 \vdots R59 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R40 \vdots R60 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R41 \vdots R61 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R42 \vdots R62 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R43 \vdots R63 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R44 \vdots R64 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R45 \vdots R65 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R46 \vdots R66 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R47 \vdots R67 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R48 \vdots R68 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R49 \vdots R69 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R50 \vdots R70 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R51 \vdots R71 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R52 \vdots R72 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R53 \vdots R73 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R54 \vdots R74 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R55 \vdots R75 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R56 \vdots R76 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R57 \vdots R77 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R58 \vdots R78 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R59 \vdots R79 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R60 \vdots R80 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R61 \vdots R81 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R62 \vdots R82 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R63 \vdots R83 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R64 \vdots R84 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R65 \vdots R85 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R66 \vdots R86 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R67 \vdots R87 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R68 \vdots R88 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R69 \vdots R89 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R70 \vdots R90 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R71 \vdots R91 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R72 \vdots R92 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R73 \vdots R93 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R74 \vdots R94 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R75 \vdots R95 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R76 \vdots R96 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R77 \vdots R97 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R78 \vdots R98 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R79 \vdots R99 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R80 \vdots R100 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R81 \vdots R101 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R82 \vdots R102 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R83 \vdots R103 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R84 \vdots R104 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R85 \vdots R105 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R86 \vdots R106 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R87 \vdots R107 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R88 \vdots R108 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R89 \vdots R109 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R90 \vdots R110 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R91 \vdots R111 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R92 \vdots R112 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R93 \vdots R113 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R94 \vdots R114 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R95 \vdots R115 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R96 \vdots R116 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R97 \vdots R117 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R98 \vdots R118 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R99 \vdots R119 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R100 \vdots R120 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R101 \vdots R121 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R102 \vdots R122 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R103 \vdots R123 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R104 \vdots R124 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R105 \vdots R125 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R106 \vdots R126 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R107 \vdots R127 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R108 \vdots R128 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R109 \vdots R129 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R110 \vdots R130 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R111 \vdots R131 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R112 \vdots R132 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R113 \vdots R133 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R114 \vdots R134 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R115 \vdots R135 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R116 \vdots R136 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R117 \vdots R137 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R118 \vdots R138 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R119 \vdots R139 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R120 \vdots R140 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R121 \vdots R141 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R122 \vdots R142 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R123 \vdots R143 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R124 \vdots R144 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R125 \vdots R145 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R126 \vdots R146 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R127 \vdots R147 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R128 \vdots R148 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R129 \vdots R149 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R130 \vdots R150 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R131 \vdots R151 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R132 \vdots R152 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R133 \vdots R153 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R134 \vdots R154 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R135 \vdots R155 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R136 \vdots R156 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R137 \vdots R157 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R138 \vdots R158 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R139 \vdots R159 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R140 \vdots R160 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R141 \vdots R161 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R142 \vdots R162 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R143 \vdots R163 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R144 \vdots R164 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R145 \vdots R165 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R146 \vdots R166 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R147 \vdots R167 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R148 \vdots R168 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R149 \vdots R169 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R150 \vdots R170 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R151 \vdots R171 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R152 \vdots R172 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R153 \vdots R173 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R154 \vdots R174 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R155 \vdots R175 $T_n^m - T_n^0$ (only aidprg) R35-44 For extra 2^{q-1}, q = 2, 4, 6..
R156 \vdots R176 T

INTEGRATION, HENRIK KLEIN, DENMARK

ARRIVAL OF THE STORM.-(v7n7/8p27) Michael Sperber is the only one so far who sent me a solution to that one. To use it: Press E' for a new storm. Enter the time in D.MS format and press A. Enter delay time between lightning and thunder in seconds and press B. Repeat often as necessary. At least two sets are required. To compute the time of arrival press C. As an example:

E' 22.3020 A 28 B ; 22.3102 A 25 B C see 22.3652
 22.3118 A 24 B C see 22.3703
 22.3210 A 20 B C see 22.3646

LBL A X:T R/S LBL B X:T DMS SUM+ R/S LBL C OP 12 INV DMS FIX 4 CP R/S
 LBL E' CMs R/S

DIGIT REVERSER 11.- At the very last moment I received two more solutions. They come from Herman Stevens in Wilsele, Belgium. Wilsele is very close to Leuven (better known outside Belgium as "Louvain") the seat of famous Catholic University, my old Alma Mater. So, I suppose Herman is a student there. Herman uses a TI-58C. One program is in Normal Mode. The second one requires Fast Mode. A 58C refuses to go into Fast mode by the sequence PGM 02 SBR 239... so Herman says to place an h12 at step 024 per his instructions below. He also used quite a lot of EE INV EE and INT and INV INT. This is absolutely necessary, as he used the method $n=\log(\text{sum of } n-1)$. This would introduce large errors in large numbers.

I am aware of the fact that the fast-mode program could be optimized, but I have no time left for the moment. Theancode at step 024 should be entered as follows : enter the first 23 steps, then in keyboardmode press GTO 24 LBN GTO BST LBN FMR 12 55P 909 2/3 17N Ins LBN RST GTO 25. Now you can enter the rest of the program.

To use the program : give the number to be reversed, press A.

Herman Stevens

000 76 Lbl	023 82 HIR	047 82 INT			031 25 CPB	063 25 +
001 11 A	024 83 6	048 05 5			032 82 HIR	064 25 ..
002 22 INV	025 22 INV	049 32 x=t			033 07 2	065 25 ..
003 38 Fix	026 85 INT	050 77 GE			034 28 HIR	066 25 ..
004 57 EXP	027 85 x	051 00 0			035 28 HIR	067 25 ..
005 82 HIR	028 85 6	052 46 36			036 26 Lbl	068 25 ..
006 06 6	029 85 6	053 52 INT			037 11 A	069 25 ..
007 23 CLR	030 82 HIR	054 38 38			038 28 HIR	070 25 ..
008 82 HIR	031 16 16	055 25 CLR			039 06 2	071 25 ..
009 62 7	032 28 LOG	056 82 HIR			040 28 x=t	072 25 ..
010 82 HIR	033 85 +	057 37 37			041 35 35	073 25 ..
011 08 2	034 00 2	058 61 370			042 01 1	074 25 ..
012 22 10	035 85 F	059 20 0			043 00 0	075 25 ..
013 22 10	036 85 INT	060 12 12			044 00 0	076 25 ..
014 22 10	037 22 INV	061 52 45P			045 00 0	077 25 ..
015 22 10	038 26 LOG	062 12 12			046 00 0	078 25 ..
016 62 82	039 85 +	063 32 37			047 82 HIR	079 25 ..
017 62 82	040 85 ..	064 22 INV			048 22 INV	080 25 ..
018 61 81	041 85 3	065 58 NOP			049 22 INV	081 25 ..
019 55 1/	042 85 3	066 85 +			050 58 INT	082 25 ..
020 01 1	043 85 INT	067 82 HIR			051 58 INT	083 25 ..
021 00 0	044 85 =	068 18 18			052 61 GTO	084 25 ..
022 00 0	045 85 x=t	069 30 30			053 00 0	085 25 ..
	046 01 1	070 92 RTN			054 30 30	086 25 ..

WANTED: James A. Girola, 1101 New Hampshire Ave. NW # 606, Washington DC 20037, Tel.: 202-566-5243, is interested in older TI and HP calculators, and would like to buy some. Members, here is your chance to make some money from those old SR-56, SR-52, and PC-100 printers lying around. Please contact Jim at the above address and phone.

DEAR MEMBERS, FRIENDS, here then comes the dreaded moment where I finally have to stop writing. So I leave you with a couple of pictures.

I will surely keep on

And for diversion, Martha and I will do some



I love you all,
James